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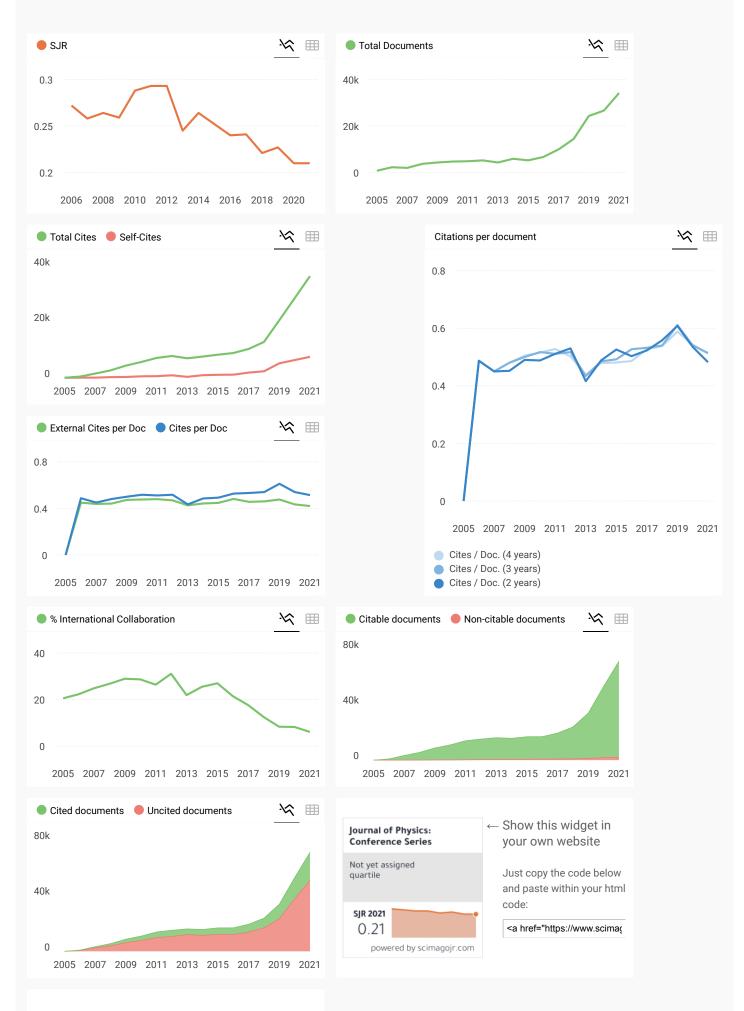
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Preface

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Preface

We are pleased and honored to welcome all presenters and participants to the First International Conference on Computer Science and Applied Mathematic (ICCSAM 2018), which was organized by AMIK and STIKOM Tunas Bangsa, Pematangsiantar, Northern Sumatera, Indonesia in collaboration with the Indonesian Computer and Information Professional Association (IPKIN), Indonesian Mathematical Society (INDOMS) and Bank Muamalat. As editors, we would like to convey a greeting Welcome to Parapat City in Lake Toba, Northern Sumatera, Indonesia to presenters from various countries and especially those we respect for the presence of scientists in the field of Computer and Mathematical Sciences and industry practitioners in the ICCSAM 2018.

We see that this activity is designed to enhance the exchange of knowledge and new discoveries in computer science and mathematics and related fields in industry. We hope that scientists in the field of computer science and mathematics and those who work in the industry can share knowledge and work together as a team that has mutual relations with each other. We are very pleased to announce that the theme of this conference, "Advancing Computability Innovation" is very much in line with the conferences objectives as well AMIK and STIKOM missions, namely "To become a Science and Technology based Study Program that meets industrial needs and functions as a research center in Information Data Science". The conference was held in response to produce significant contribution in the field of computer science and mathematics as an inseparable unit of science towards the development of local and global industries. It is our happiness and honor to welcome distinguished professors present to convey their expertise at this conference.

We hope this meeting will enable the development of productive dialogue between participants from various countries. They also provide invaluable opportunities for networking among participants, institutions and industries. We also hope that diversity in these fields can reveal more opportunities for researchers and practitioners from all over the world to start a lot of research related to the industry in the future.

We would like to congratulate AMIK and STIKOM Tunas Bangsa for starting this conference with a synergistic contribution from dedicated partners namely the Faculty of Mathematics and Natural Sciences of Universitas Sumatera Utara, Faculty of Computer and Information Technology of Universitas Sumatera Utara, the Indonesian Computer and Informatics Professional Association (IPKIN), Indonesian Mathematical Society (INDOMS), Bank Muamalat, Malaysia Pahang University (UMP), University of Essex UK, Ankara, Institute of Applied Mathematics, Middle East Technical University, Turkey and to all delegates for their full support, cooperation and contribution to the ICCSAM 2018. We also want to thank the Organizing Committee for their perseverance and extraordinary efforts. Various sponsors are also rewarded for their contributions. We finally hope that all participants will get a pleasant stay here at Niagara Hotel and bring back unforgettable experiences and valuable knowledge from this conference.

Editors

Ahmad Ridwansyah Putra Dedy Hartama Agus Perdana Windarto Anjar Wanto Sajadin Sembiring Tutut Herawan

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Randomized quasi Monte Carlo methods for pricing of barrier options under fractional Brownian motion

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Abstract. Randomized quasi-Monte Carlo (RQMC) method is presented to compute the problem of a barrier option pricing. It is assumed that stock prices are modeled with a fractional Brownian motion (FBM). The FBM is a Gaussian process with dependent and stationary increments except $H = \frac{1}{2}$. The FBM can model stock prices with short or long memory. We propose a trajectory generation technique based on fast Fourier transforms to simulate stock prices modeled by FBM. A stock price trajectory is utilized to predict pricing of barrier options. Barrier options are options whose payoff function depend on the stock prices during the option's lifetime. Using the results of the stock price trajectory and RQMC method can be determined the price of a barrier option under FBM. We conclude that RQMC is an efficient technique for calculating the price of barrier options rather than a standard Monte Carlo (MC).

1. Introduction

Monte Carlo (MC) method is one way that can overcome financial problems, especially in determining option prices. MC method is a method that uses random numbers to determine an expected value of a random variable. These random numbers are pseudo-random numbers (PRN) that have a certain probability distribution. However, this method has a slow speed of convergence and rather time-consuming, because a root of the average decay error is $O(N^{-1/2})$, where N is a number of samples.

Quasi-Monte Carlo (QMC) method is an efficient alternative to the standard MC method, which is able to achieve faster convergence and higher accuracy [1,2]. The QMC method is based on using a low-discrepancy sequence (LDS), is also called a quasi-random number for sampling point. LDS is designed so that the integration domain resembles a uniform distribution but the process of determining random numbers is deterministic. However, PRN is a random number that has a uniform distribution and fulfills statistical properties.

With deterministic QMC method, it is difficult to estimate integration errors in practice. Randomized quasi-Monte Carlo (RQMC) method is used to replace QMC method. RQMC method combines LDS and PRN. In this paper, Halton and Sobol sequence, which are LDS with a different deterministic model, will be applied in ROMC method for calculating a barrier option pricing.

Analytical formulas for calculating barrier options are not available in many cases such as barrier options under the FBM model and options with many assets. The MC method is one that plays an

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important role in this situation. The MC algorithm is an algorithm based on simulating several stock price trajectories under a risk-neutral probability measure. A price of barrier options with the MC method has been discussed at [3–6]. Meanwhile, the price of barrier options under the FBM model using RQMC method has never been discussed. The purpose of this paper is to determine the price of a barrier option using RQMC method.

2. Fractional Brownian motion

An FBM $B^{H} = (B_{t}^{H})_{t \ge 0}$ is a Gaussian process with a zero mean and a covariance function is defined

$$\mathbf{E}\left[B_{t}^{H}B_{u}^{H}\right] = \frac{1}{2}\left(\left|t\right|^{2H} - \left|t - u\right|^{2H} + \left|u\right|^{2H}\right),\tag{1}$$

where Hurst index $H \in (0, 1)$ and $t, u \ge 0$, see [7]. More precisely, by using (1), we obtain that covariance between $X_t = B_t^H - B_{t-1}^H$ and $X_{t+u} = B_{t+u}^H - B_{t+u-1}^H$ is

$$\rho_H(u) = \frac{1}{2} \Big((u-1)^{2H} - 2u^{2H} + (u+1)^{2H} \Big).$$
⁽²⁾

A FBM coincides with a standard BM if $H = \frac{1}{2}$. The Hurst index H determines the sign of the covariance of the future and past increments. This covariance is negative when $H \in (0, \frac{1}{2})$, positive when $H \in (\frac{1}{2}, 1)$, and zero when $H = \frac{1}{2}$. As a consequence, it has short-range dependence (short memory) for $H \in (0, \frac{1}{2})$ and it has long-range dependence (long memory) for $H \in (\frac{1}{2}, 1)$.

The stock price model under the FBM is given by

$$dS_{t} = \mu S_{t} dt + \sigma S_{t} d\hat{B}_{t}^{H}, \qquad t \in [0, T], S_{0} > 0,$$
(3)

where μ and σ are constants, \hat{B}_{t}^{H} is the FBM with respect to \hat{P}^{H} . The fractional Black-Scholes model consists of one riskless asset (bank account) and one risk asset (stock). The stock price satisfies a stochastic differential equation (3). By using a change of variable $\sigma \hat{B}_{t}^{H} = \sigma B_{t}^{H} - \mu + r$ and using the Girsanov theorem in [7], we have

$$dS_t = rS_t dt + \sigma S_t dB_t^H, \qquad t \in [0, T], S_0 > 0.$$
(4)

Furthermore, we obtain a solution of (4) as

$$S_t = S_0 \exp\left(rt + \sigma B_t^H - \frac{1}{2}\sigma^2 t^{2H}\right),\tag{5}$$

by using a Itô formula in [7].

3. Pricing of barrier options

Path-dependent options are options whose value depends on a behavior of stock prices during its lifetime. Unlike vanilla options, the price of path-dependent options depends not only on a stock price at maturity but also on stock prices trajectory during the contract. There are many types of path-dependent options, such as Asian options, lookback options, and barrier options. Each option has unique characteristics. Path-dependent options offer premium prices that are cheaper than the standard vanilla option.

A barrier option is a option that can be activated or deactivated if the stock price reaches a certain price level (*L*). Barrier options in general consist of two types, namely knock in and knock out options. A knock out option is an option whose contract is canceled if the stock price crosses the barrier value. A knock in option, on the other hand, is activated if the stock price crosses the barrier value. The relationship between a barrier value *L* and a current stock price S_0 indicates whether the option is an up or down option. We have an up option if $L > S_0$ and we have a down option if $L < S_0$. Combining the payoffs of call and put options with these features, we can define an array of barrier options.

An option is said to be an up-and-out option if the stock price crosses a barrier value and the value is greater than the current stock price. A down-and-out option is an option which the stock price crosses a barrier value and the value is below the current stock price. The payoff of an up-and-out call option with barrier value L, expiration time T and strike price K, is given by

$$f(S_T) = (S_T - K)^+ \mathbf{1}_{\sup_{t \in [0,T]} \{S_t \le L\}}$$
(6)

and the payoff of a down-and-out call option is given by

$$f(S_T) = (S_T - K)^+ \mathbf{1}_{\sup_{t \in (0,T)} \{S_t \ge L\}}$$
(7)

The payoff function of a put option is defined similarly with $(K - S_T)^+$ in place of $(S_T - K)^+$.

A closed form formula for an option barrier pricing under a fractional Brownian motion model has not been found. This is because a fractional Brownian motion no longer has markovian and martingale properties so the reflective principle used to derive formulas for barrier options is no longer valid. So it is difficult to get an analytical solution from the barrier option pricing.

4. Randomized quasi Monte Carlo

Option pricing using the MC method can be determined in the following three stages

- Simulate sample trajectories from stock prices during a time interval [0, T] as many as m times,
- Calculate a discounted expected value of a payoff function of a barrier option for each trajectory that generated in the first stage,
- Average the value that calculated in the second stage.

In the vanilla option, there is actually no need to make a stock price trajectory, only the stock price at maturity is of concern. Barrier options are options that depend on the trajectory of a stock prices. The barrier option pricing is determined by whether the stock price passes a certain barrier value during the option period. Because of this path-dependent, all stock price simulations are needed during the option period. To simulate a sample trajectory, we must choose a stochastic differential equation that illustrates price dynamics. Stochastic equations for a stock price under FBM are written in (5).

QMC simulation is based on the same procedure as MC simulation but uses LDS instead of PRN. Similar to PRN, LDS is algorithmically generated by a computer, except that the LDS is determined deterministically in a smart way to be more uniformly distributed than PRN. In contrast to an MC sample, LDS do not have the independent and identically distributed (i.i.d.) property.

Therefore, we cannot directly use LDS in the QMC method. However, randomized LDS samples can be constructed by changing LDS into the following form

$$\tilde{U}_i = (U_i + W_i) \mod 1, \tag{8}$$

where W_i is a PRN and U_i is an LDS. The vector \tilde{U}_i is uniformly distributed in the unit hypercube and sequence \tilde{U} have the independent and identically distributed property. Thus, the estimators based on \tilde{U}_i are unbiased.

The best known quasi-random number generations [8] are Halton sequences, Faure sequences, Sobol sequences, and the lattice method. This paper only discusses two quasi-random number generations, namely Sobol sequences and Halton sequences. Sobol sequences are examples of LDS. Ilya M Sobol, a Russian mathematician, first introduced Sobol sequences [9] in 1967. Sobol points can be produced using algorithms introduced by Bratley and Fox [10]. Halton Sequences are sequences that produce points in space using numerical methods such as appear to be random. The Halton sequence was first introduced in 1964 [11] and developed by Kocis and Whiten [12].

5. Numerical Results

In this section, we first simulate sample trajectories from stock prices at time intervals [0, T]. The stock price is modeled using equation (5). The algorithm for building trajectories of stock prices using quasi random numbers is seen in Algorithm 1. Using the algorithm can be generated trajectories of

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stock prices like Figure 1. Figure 1 also says that when H = 1/2, the FBM will be the same as the standard BM.

input : Set an expire date T, an initial stock price S_0 , an interest rest r, a stock volatility σ , a Hurst index H and a large number n of equally spaced subintervals in [0, T)**output:** S_t with $t = t_1, t_2, ..., t_n \in [0, T)$ 1 Set using pseudo random number, Halton sequences or Sobol sequences; **2** for $j \leftarrow 1$ to n do Generate two pseudo-random number W_{1i} and W_{2i} ; 3 if pseudo random number then 4 $\tilde{U}_{1i} \longleftarrow W_{1i}$ and $\tilde{U}_{2i} \longleftarrow W_{2i}$; 5 else 6 Generate two two Halton or Sobol sequences U_{1j} and U_{1j} ; 7 $\tilde{U}_{1j} \longleftarrow (U_{1j} + W_{1j}) \mod 1 \text{ and } \tilde{U}_{2j} \longleftarrow (U_{2j} + W_{2j}) \mod 1;$ 8 end 9 RandomComplex $\leftarrow \tilde{U}_{1j} + \tilde{U}_{2j} i;$ 10 11 end 12 $\rho(1) = 1;$ 13 for $k \leftarrow 1$ to n do $\rho_{k+1} \longleftarrow \frac{1}{2} \left((k-1)^{2H} - 2k^{2H} + (k+1)^{2H} \right);$ 14 15 end 16 ρ new $\leftarrow [\rho; \rho(end - 1: -1: 2)]$ 17 $\lambda \leftarrow \frac{\text{Real}(\text{FFT}(\rho \text{ new}))}{2\pi n}$ 2*n $X \leftarrow \text{FFT}\left(\sqrt{\lambda}\right) * \text{RandomComplex}$ 18 19 $W \leftarrow \text{CUMSUM}(\text{Real}(X(1:n+1))))$ **20** for $j \leftarrow 1$ to n do $S_{t_j} \leftarrow S_0 \exp\left(r\frac{jT}{n} - \frac{1}{2}\sigma^2\left(\frac{jT}{n}\right)^{2H} + \sigma\left(\frac{T}{n}\right)^H W_j\right)$ 21 22 end

Algorithm 1. Stock price trajectories under FBM

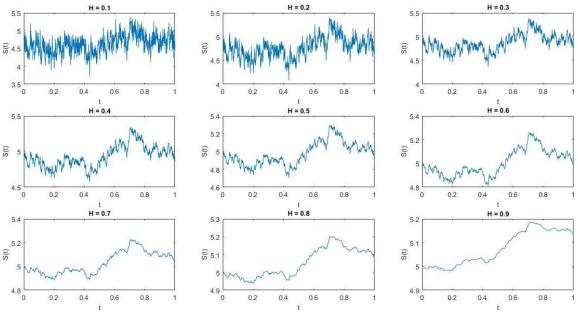


Figure 1. Stock price trajectories under FBM by using Sobol sequences

If $H < \frac{1}{2}$ the trajectory of the stock price fluctuates greatly, and if $H > \frac{1}{2}$ the trajectory of the stock price is more likely to be smooth.

Algorithm 2 is an algorithm used to calculate the pricing of a barrier option under an FBM model using MC and RQMC. The pricing of a barrier option can be determined using the trajectory of stock prices generated in Algorithm 1. The pricing of a barrier option generated in Algorithm 2 is an up-and-out call option. Other barrier options can be calculated by changing lines 4-6 in Algorithm 2 according to the payoff function of the option. All algorithms in this paper are written and executed in the Matlab program.

input : Set an expire date T, a strike price K, an initial stock price S_0 , a interest rest r, a stock volatility σ , a Hurst index H, a large number n of equally spaced subintervals in [0, T) and sample size m output: Price of an up-and-out call option 1 Set using pseudo random number, Halton sequences or Sobol sequences **2** for $j \leftarrow 1$ to m do Set $S_T \leftarrow$ stock price trajectory using Algoritma 1 3 $S_{Max} \leftarrow \max \{S_t | S_t \in S_T \text{ and } t \in (0, T)\}$ 4 if $S_{Max} < L$ then 5 $V_j \leftarrow \exp(-rt) \max\{S_T(\text{end}) - K, 0\}$ 6 7 else 8 $V_j \leftarrow 0$ end 9 10 end 11 $C_m \leftarrow \sum_{j=1}^m V_j / m$

Algorithm 2. Price of an up-and-out call option using randomized quasi Monte Carlo

We present an example to show the effectiveness of Algorithm 2. We use current stock price $S_0 = 500$, strike price K = 500, expiration date T = 1, stock volatility $\sigma = 0.05$, index Hurst H = 0.8, and interest rate r = 0.05. We implement the MC and RQMC simulation algorithms and compare the results obtained from all methods. The RQMCS method is the RQMC method while the LDS used is the Sobol sequence. Whereas, the RQMCH method is the RQMC method by using the Halton sequence.

			<u> </u>	<u> </u>			
М	MN		up-and-out c	all option	Error	of an option	price
M N	IN	MC	RQMCS	RQMCH	MC	RQMCS	RQMCH
100	1000	17,24898	14,07713	13,99044	1,52361	0,94219	1,01528
1000	1000	14,49144	14,97568	15,00420	0,47331	0,32219	0,32139
10000	1000	15,09796	15,23683	15,15125	0,15128	0,10101	0,10141
100000	1000	15,27597	15,29528	15,23070	0,04809	0,03201	0,03199

Table 1. Price of an up-and-out call option with $M = 10^2$, 10^3 , 10^4 , 10^6

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	Table 2. Frice of an up-and-out can option with $N = 10$, 10, 10, 10							
М	Ν	Price of an up-and-out call option			Error of an option price			
IVI	IN	MC	RQMCS	RQMCH	MC	RQMCS	RQMCH	
1000	100	14,38474	14,97417	15,97086	0,47787	0,32375	0,31689	
1000	1000	15,20676	14,74686	15,41580	0,48841	0,32536	0,32023	
1000	10000	15,53449	14,98866	14,44457	0,48684	0,31704	0,31358	
1000	100000	15,13752	15,30209	15,23531	0,47789	0,32155	0,32103	

Table 2. Price of an up-and-out call option with $N = 10^2$, 10^3 , 10^4 , 10^6	Table 2	. Price of an	up-and-out call	option with N	$V = 10^2$,	$10^3, 10^4, 10^6$
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6. Conclusion

One of the methods to determine the pricing of a barrier option under an FBM model is to use the RQMC methods. The stock price trajectory under the FBM model has been proposed in Algorithm 1. Using Algorithm 1 can be determined the barrier option price under the FBM model with the MC and RQMC methods described in Algorithm 2. We compare the accuracy of MC and RQMC method in the pricing of barrier option under the FBM model. The RQMC method more efficient than the MC method which is shown by smaller errors.

Acknowledgments

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