

Search Sources Lists SciVal 7

?

Д

ΑН

**①** 

**(i)** 

**(i)** 

### Source details

Journal of Physics: Conference Series

Scopus coverage years: from 2005 to Present

ISSN: 1742-6588 E-ISSN: 1742-6596

Subject area: (Physics and Astronomy: General Physics and Astronomy)

Source type: Conference Proceeding

View all documents >

Set document alert

■ Save to source list Source Homepage

SJR 2020 **0.210** 

CiteScore 2020

0.7

SNIP 2020 **0.464** 

CiteScore

CiteScore rank & trend

Scopus content coverage

Improved CiteScore methodology

CiteScore 2020 counts the citations received in 2017-2020 to articles, reviews, conference papers, book chapters and data papers published in 2017-2020, and divides this by the number of publications published in 2017-2020. Learn more >

CiteScore 2020 ~

 $0.7 = \frac{52,411 \text{ Citations } 2017 - 2020}{72,842 \text{ Documents } 2017 - 2020}$ 

Calculated on 05 May, 2021

CiteScoreTracker 2021 ①

 $0.8 = \frac{72,838 \text{ Citations to date}}{96,860 \text{ Documents to date}}$ 

Last updated on 06 March, 2022 • Updated monthly

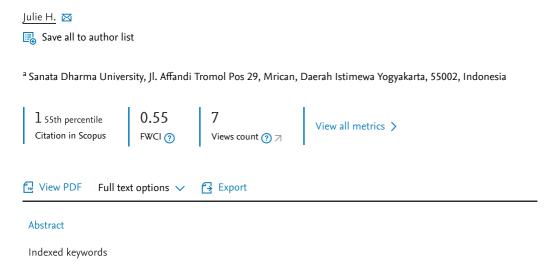
### CiteScore rank 2020 ①

Category	Rank	Percentile
Physics and Astronomy General Physics and Astronomy	#191/233	18th

View CiteScore methodology > CiteScore FAQ > Add CiteScore to your site &



# Developing LTBI for addition and multiplication rules in probability theory with realistic mathematics education



### Abstract

Metrics

SciVal Topics

Sustainable Development Goals 2021

There were three components on a hypothetical learning trajectory (HLT) developed in this paper, namely: (1) the learning goal, (2) the learning activities, and (3) the way of students' thinking and learning. A learning trajectory based instruction (LTBI) was defined as a teaching and learning trajectory using HLT for instructional decisions. In this paper, the researcher will present a LTBI using Realistic Mathematics Education approach which helps mathematics education students following the Probabilistic Theory course to construct (1) the addition rule, and (2) the multiplication rule. The type of the research was the design research developed by Gravemeijer and Cobb. There were three phases in the research development, namely (1) the design preparation, (2) the design trial, and (3) the retrospective analysis. The researcher exposure in this paper was limited to the first stage of the design research developed by Gravemeijer and Cobb. As the products developed in this paper was limited to LTBI, so to construct a local instructional theory (LIT) for the sum and multiplication rules, the

### Cited by 1 document

Analysis of problem-solving skills in material probability in Kanisius Pakem vocational high school

Gunawan, F.I., Lagut, N.M. (2020) Journal of Physics: Conference Series

View details of this citation

Inform me when this document is cited in Scopus:

Set citation alert >

### Related documents

The Mathematical Literacy Teachers' Ability for Quantity Area on PISA Adaptation Test

Julie, H., Sanjaya, F., Anggoro, A.Y. (2018) Journal of Physics: Conference Series

The teacher's mathematical literacy for the change and relationship problems on the PISA adaptation test

Anggoro, A.Y. , Julie, H. , Sanjaya, F.

(2018) Journal of Physics: Conference Series

The mathematics education department students' ability in mathematical literacy for the change and relationship problems on the PISA adaptation

Anggoro, A.Y., Julie, H., Sanjaya, F.

(2019) Journal of Physics: Conference Series

View all related documents based on references

Find more related documents in Scopus based on:

Author > Keywords >

Indexed keywords		~
Sustainable Devel	opment Goals 2021 ① New	~
SciVal Topics (i)		~
Metrics		~
	References (12) View in search results for	ormat )
	☐ All CSV export ✓ ☐ Print ☒ E-mail ∰ Save to PDF	
	Create bibliography	
	☐ 1 Julie, H. (2017) AIP Conference Proceedings Vol 1868 (US: AIP Publishing)	
	2 Sztajn, P., Confrey, J., Wilson, P.H., Edgington, C.	
	Learning Trajectory Based Instruction: Toward a Theory Teaching	of
	(2012) Educational Researcher, 41 (5), pp. 147-156. Cited 112 times. doi: 10.3102/0013189X12442801	
	View at Publisher	
	☐ 3 Simon, M.A.  Reconstructing mathematics pedagogy from a constructivist perspecti (1995) Journal for Research in Mathematics Education, 26, p. 114. Cite times.	
	Campbell, P.F., Nishio, M., Smith, T.M., Clark, L.M., Conant, D.L., Rus A.H., DePiper, J.N., (), Choi, Y.	t,
	The relationship between teachers'mathematical content pedagogical knowledge, teachers' perceptions, and studiachievement	
	(2014) Journal for Research in Mathematics Education, 45 (4), pp. 419-459. Cited 70 times. <a href="http://www.nctm.org/publications/archive.aspx?jrnl=jrme">http://www.nctm.org/publications/archive.aspx?jrnl=jrme</a>	
	doi: 10.5951/jresematheduc.45.4.0419  View at Publisher	
	☐ 5 Julie, H.  The elementary school teachers' ability in adding and subtracting fract and interpreting and computing  (2017) International Journal of Science and Applied Science: Conference Series, 1, p. 55. Cited 7 times.	
	<ul> <li>6 Skemp, R.</li> <li>(2009) The Psychology of Learning Mathematics. Cited 495 times.</li> <li>(New York: Routledge)</li> </ul>	

_ 7	Wijaya, A.  Students' information literacy: A perspective from mathematical literacy (Open Access)
	(2016) Journal on Mathematics Education, 7 (2), pp. 73-82. Cited 22 times. <a href="https://ejournal.unsri.ac.id/index.php/jme/article/view/3532/1875">https://ejournal.unsri.ac.id/index.php/jme/article/view/3532/1875</a> doi: 10.22342/jome.v7i2.3532
	View at Publisher
□ 8	Stacey, K.  The PISA view of mathematical literacy in Indonesia (Open Access)
	(2011) Journal on Mathematics Education, 2 (2), pp. 95-126. Cited 102 times. <a href="https://ejournal.unsri.ac.id/index.php/jme/article/view/746/200">https://ejournal.unsri.ac.id/index.php/jme/article/view/746/200</a> doi: 10.22342/jme.2.2.746.95-126
	View at Publisher
□ 9	Gravemeijer, K.P.G. (1994) <i>Developing Realistic Mathematics Education</i> . Cited 342 times. (Utrecht: Freudenthal Institute)
□ 10	Julie, H. Student learning materials on the multiplication and division of fractions for grade five with realistic mathematics education (2015) <i>Proceedings of the 3th SEA-DR Conference</i> . Cited 3 times. (Palembang: Universitas Sriwijaya)
☐ 11	Julie, H.  (2016) Developing Student Learning Materials on the Multiplication Fractions for Grade Five with Realistic Mathematics Education Proceedings of the 4th SEA-DR Conference (Padang: Universitas Negeri Padang)
<u> </u>	Van Den Akker, J., Gravemeijer, K., McKenney, S., Nieveen, N. (2006) <i>Educational Design Research</i> . Cited 468 times. (New York: Routledge)
Istimewa	H.; Sanata Dharma University, Jl. Affandi Tromol Pos 29, Mrican, Daerah Yogyakarta, Indonesia; email:hongkijulie@yahoo.co.id ight 2018 Elsevier B.V., All rights reserved.

### **About Scopus**

What is Scopus

Content coverage

Scopus blog

Scopus API

Privacy matters

### Language

日本語に切り替える

切换到简体中文

切換到繁體中文

Русский язык

### **Customer Service**

Help

Tutorials

Contact us

### **ELSEVIER**

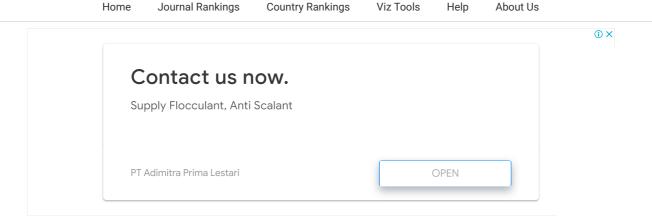
Terms and conditions  $\ \ \,$  Privacy policy  $\ \ \,$ 

Copyright © Elsevier B.V 对. All rights reserved. Scopus® is a registered trademark of Elsevier B.V.

We use cookies to help provide and enhance our service and tailor content. By continuing, you agree to the use of cookies.



Enter Journal Title, ISSN or Publisher Name



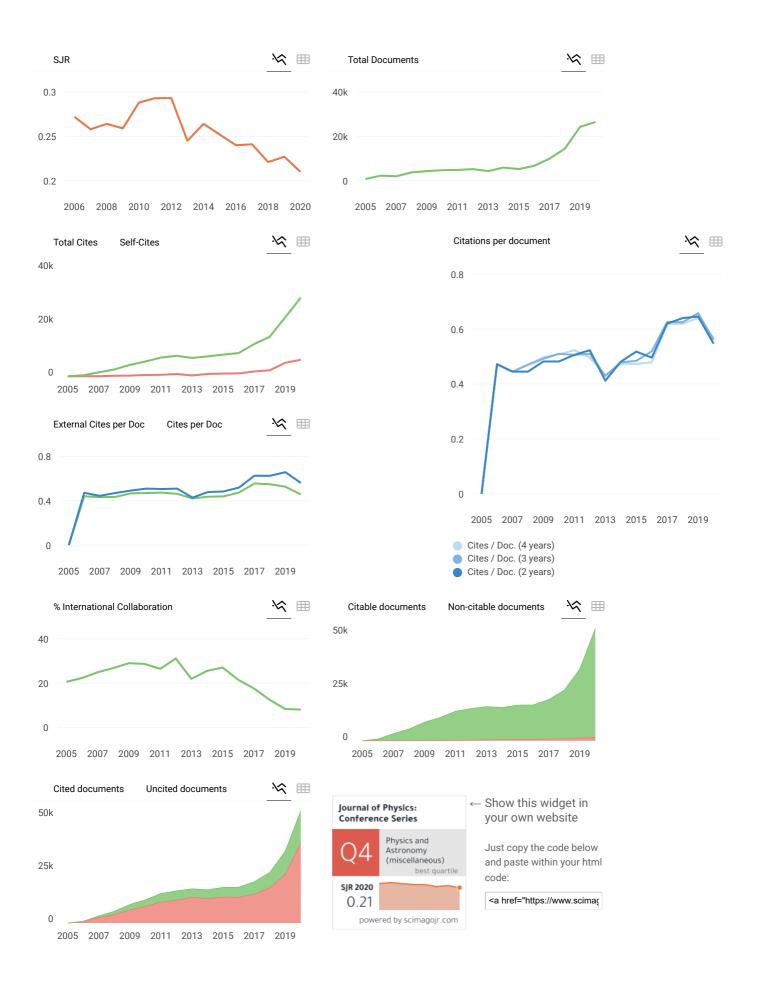
### **Journal of Physics: Conference Series 3**

COUNTRY	SUBJECT AREA AND CATEGORY	PUBLISHER	H-INDEX
United Kingdom  Universities and research institutions in United Kingdom	Physics and Astronomy Physics and Astronomy (miscellaneous)	IOP Publishing Ltd.	85
PUBLICATION TYPE	ISSN	COVERAGE	INFORMATION
Conferences and Proceedings	17426588, 17426596	2005-2020	Homepage  How to publish in this journal  jpcs@ioppublishing.org

### SCOPE

The open access Journal of Physics: Conference Series (JPCS) provides a fast, versatile and cost-effective proceedings publication service.

 $\bigcirc$  Join the conversation about this journal





Metrics based on Scopus® data as of April 2021

### Z Zainab 4 weeks ago

hello, is the IOP Journal of Physics: Conference Series of this journal listested in scopus?

reply



### Melanie Ortiz 4 weeks ago

SCImago Team

Dear Zainab, thank you very much for your comment. We suggest you consult the Scopus database directly. Keep in mind that the SJR is a static image (the update is made one time per year) of a database (Scopus) which is changing every day.

Best Regards, SCImago Team

### D Dr Girisha A 1 month ago

Dear sir,

Please inform me, whether Journal of Physics: Conference Series 1767 (2021) 012011 is rated in Q3 0r Q4.

reply



### Melanie Ortiz 4 weeks ago

SCImago Team

Dear Dr Girisha,

Thank you for contacting us. Please see comments below.

Best Regards, SCImago Team

### N narasiman 2 months ago

Dear sir,

### **PAPER • OPEN ACCESS**

## The 6th South East Asia Design Research International Conference (6th SEA-DR IC)

To cite this article: 2018 J. Phys.: Conf. Ser. 1088 011001

View the article online for updates and enhancements.

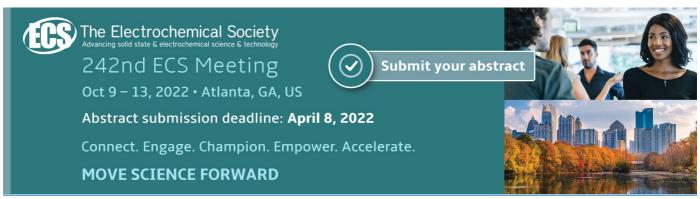
### You may also like

- The condition of reef fish (family Chaetodontidae) in Krueng Raya and Ujong Pancu waters, Aceh Besar District C Octavina, M Ulfah, M R Fazillah et al.
- Geochemistry of Sulphate spring in the le Jue geothermal areas at Aceh Besar district, Indonesia

R Idroes, M Yusuf, M Alatas et al.

- Activities inhibition methanol extract Laban Leaf (Vitex pinnata) on growth of bacteria S. mutans Atcc 31987

C A Nuraskin, Marlina, R Idroes et al.



# The 6<sup>th</sup> South East Asia Design Research International Conference (SEA-DR IC) 2018

R Johar<sup>1</sup>, C Morina<sup>1</sup>, Anwar<sup>1</sup>, Mailizar<sup>1</sup>, Elizar<sup>1</sup>, C Khairunnisak<sup>1</sup>, R C I Prahmana<sup>2</sup>, W Artika<sup>1</sup>, L Vitoria<sup>1</sup>, L Khairi<sup>1</sup>, S Maulina<sup>1</sup> and M Ulfa<sup>1</sup>

E-mail: rahmahjohar@fkip.unsyiah.ac.id

### **Preface**

The South East Asia Design Research (SEA-DR) as a forum of design research in collaboration with Master Program of Mathematics Education, Syiah Kuala University, organized the 6th SEA-DR conference with the theme "Inspiring students to learn: Fostering innovative teaching and learning of science, mathematics and technology".

This conference was an excellent opportunity for academics, researchers, teachers and students to share knowledge, experiences and research findings as well as to inspire the best practice of development research in the field of teaching mathematics, science, and technology.

We had four keynote speakers that were Prof. Berinderjeet Kaur, Prof. Maarten Dolk, Prof. Lilia Halim, and Dr. John Willison. We also had ten invited speakers and four keynote speakers in workshop sessions. Furthermore, there were 181 papers, including 148 oral presentation and 33 posters presentations. The 6th SEA-DR conference successfully attracted delegates from many countries. There were seven countries participating in this conference, including: Singapore, the Netherlands, Denmark, Australia, Malaysia, Brunei Darussalam, and Indonesia.

Finally, we would like to extend our gratitude for everyone involved for their contribution in the conference.

<sup>&</sup>lt;sup>1</sup>Syiah Kuala University, Banda Aceh, 23111, Indonesia

<sup>&</sup>lt;sup>2</sup>Universitas Ahmad Dahlan, Jl. Pramuka Kav. 5, Yogyakarta 55161, Indonesia

Content from this work may be used under the terms of the Creative Commons Attribution 3.0 licence. Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI.

### The Committee of 6<sup>th</sup> South East Asia Design Research International Conference (SEA-DR IC) 2018

### **Steering Committee**

Prof. Dr. Ir. Samsul Rizal, M. Eng (Rector of Syiah Kuala University)

Prof. Dr. Djufri, M. Si (Dean of FKIP Syiah Kuala University)

Prof. Dr. Maarten Dolk

Prof. Dr. R.K Sembiring

Dr. Y. Marpaung

Prof. Dr. Zulkardi, M. I. Kom, M.Sc.

Prof. Dr. Sutarto Hadi, M.Si., M. Sc.

Prof. Dr. Dian Armanto, M.Pd, M.Sc.

Prof. Dr. Ahmad Fauzan, M.Pd, M. Sc.

Prof. Dr. Turmudi, M.Ed, M.Sc.

Dr. M. Ikhsan, M.Pd. (Head of Mathematics Education Department of Syiah Kuala Univesity)

Prof. Berinderjeet Kaur

Prof. Lilia Halim

### **Organizing Committee**

Conference Chair : Dr. Rahmah Johar, M.Pd.

Conference Co-Chair : Dr. Anwar, M.Pd. Secretary : Dr. Mailizar, M.Ed.

Vice Secretary : Elizar, Ph.D.

Treasurer : Dr. Cut Morina Zubainur, M.Pd.

Vice Treasurer : Suhartati, M.Pd.

### **Scientific Committee**

Scientific Committee Chair : Prof. Dr. Marwan, M. Si

Scientific Committee Member :

Prof. Maarten Dolk

Prof. Rohaida Mohd. Saat

Prof. Dr. Musri Musman, M.Sc.

Prof. Dr. Ratu Ilma Indra Putri, M.Si.

Prof. Dr. Muchlisin Z.A, M.Sc.

Prof. Dr. Adlim, M.Sc.

Prof. Dr. Ahmad Fauzan, M.Sc.

Dr. Cathy Wissehr

Dr. Wanty Widjaja

Dr. Abdul Halim Abdullah

Dr. Ariyadi Wijaya, M.Sc.

Dr. Al Jupri, M.Sc.

Dr. Tatag Yuli Eko Siswono, M.Pd.

Dr. Yenita Roza, M.Sc.

Dr. Shintia Revina, M.Sc.

Dr. Neni Mariana, M.Sc.

Dr. Rooselina Ekawati, M.Sc.

Dr. Nasrullah Idris, M.Eng.

Dr. Hongki Julie, M.Pd.

Dr. Taufik Fuadi Abidin, M.Tech.

Dr. Rully Charitas Indra Prahmana

Dr. Supriatno, M.Si. Dr. Said Munzir, M.Eng.Sc. Dr. Suhartono, M.Sc. Aysenur Alp Zarlaida Fitri, M.Sc. Veronika Fitri Rianasari, M.Sc. Meliasari., M.Sc. Zetra Hainul Putra, M.Sc. Destina Wahyu Winarti, M.Sc. Fridgo Tasman, M.Sc. Fatimatul Khikmiyah, M.Sc. Achmad Badrun Kurnia, M.Sc. Mulia Putra, M.Pd., M.Ed. Rita Novita, M.Pd. Bustang Buhari, M.Sc. Intan Kemala Sari, M.Pd.

### **Keynote Speakers**

Prof. Berinderjeet Kaur National Institute of Education, Singapore

Prof. Maarten Dolk Utrecht University, the Netherlands

Prof. Lilia Halim University Kebangsaan Malaysia, Malaysia

Dr. John Willison the University of Adelaide, Australia

### Table of contents

### Volume 1088

### September 2018

◆ Previous issue Next issue ▶

The 6th South East Asia Design Research International Conference (6th SEA-DR IC)27–28 June 2018, Banda Aceh, Indonesia

Accepted papers received: 17 August 2018

Published online: 19 October 2018

Open all abstracts

Preface			
OPEN ACCESS			011001
The 6th South Ea	ast Asia Design Res	earch International Conference (6th SEA-DR IC)	
+ Open abstract	View article	PDF	
OPEN ACCESS			011002
Peer review state	ment		
+ Open abstract	View article	PDF	
Papers			
OPEN ACCESS			012001
The effectiveness	s of STEM mentorii	ng program in promoting interest towards STEM	
L Halim, T M T So	h and N M Arsad		
+ Open abstract	View article	PDF	
OPEN ACCESS			012002
How do we let st	udents work as 'you	ing mathematicians' in the classroom?	
M Dolk			
+ Open abstract	View article	PDF	

OPEN ACCESS 012003

0

+ Open abstract	View article	PDF	
OPEN ACCESS			012034
	crosoft Excel as an	n interactive learning media of acid-base titration	012034
I Khaldun, M Hasan	and Nilawati		
+ Open abstract	View article	PDF	
OPEN ACCESS		a amotical locumina	012035
	earning resources in Elizar, R Johar and T I		
	View article		
+ Open abstract	view article	PDF	
OPEN ACCESS The validity of ve	ctor analysis modu	le using wxMaxima software	012036
Khairina, M Ikhsan	•	ic using winaxima software	
+ Open abstract	View article	₱ PDF	
+ Open abstract	= View article		
OPEN ACCESS			012037
Difficulties analys	sis of mathematics	education students on the real analysis subject	
I Widiati and A Sthe	phani		
+ Open abstract	View article	PDF	
OPEN ACCESS			012038
The development students' problem-	_	nents based on an open-ended approach to improve	
N R Fandanu, M Ikh	nsan and Bahrun		
+ Open abstract	View article	PDF	
OPEN ACCESS The development	of learning materia	als using contextual teaching learning (CTL)	012039
1	on the character ed		
R Johar, Agussalim,	M Ikhsan and B Zaur	ra	
+ Open abstract	View article	PDF	
OPEN ACCESS			012040
Developing learni approach	ng trajectory for te	aching statistics at junior high school using RME	
A Fauzan, E Musdi	and J Afriadi		
+ Open abstract	View article	PDF	

This site uses cookies. By continuing to use this site you agree to our use of cookies. To find out more, See our Privacy and Cookies policy.

0120

Y Fitria, Y Heisa, F	i Nirwana and A P Zu	ikarnaini	
+ Open abstract	View article	PDF	
OPEN ACCESS The practicality of Angry Birds game	•	ction module by utilizing Autograph Software and	012042
C M Zubainur, Suh	artati and Iwannitona		
+ Open abstract	View article	₹ PDF	
OPEN ACCESS			012043
Development of a	algebra test question	ns based on Bloom's taxonomy	
M Husna, R Johar,	Hajidin and Mailizar		
+ Open abstract	View article	₹ PDF	
OPEN ACCESS Developing LTB! mathematics educ		nultiplication rules in probability theory with realistic	012044
H Julie			
+ Open abstract	View article	PDF	
to train the <i>mural</i> .  S Hartini, M F Isna	kata character nda, M Wati, M Misba	on the local wisdom of Hulu Sungai Tengah regency	012045
+ Open abstract	View article	PDF	
-	•	ces through Benthic species study in mangrove vertebrate zoology learning	012046
M Ali S, Supriyatno	o, M D Asiah, M Sapu	tri, A Mursawal and Zulfikar	
+ Open abstract	View article	PDF	
OPEN ACCESS			012047
PISA-like mather	matics problems us	ing the context of athletics in Asian Games 2018	
I Pratiwi, R I I Putr	i and Zulkardi		
+ Open abstract	View article	PDF	
OPEN ACCESS			012048
-		the context of <i>timpan</i> recipes	
Thiszing and see our Privacy and		se this site you agree to our use of cookies. To find out more,	8

The integration of science and math

### **PAPER • OPEN ACCESS**

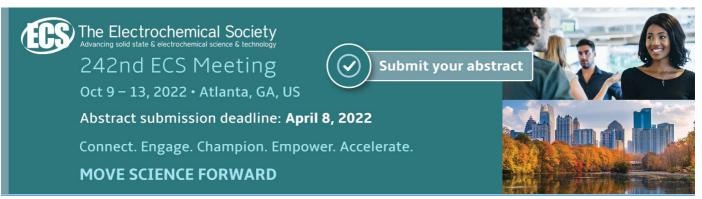
# Developing LTBI for addition and multiplication rules in probability theory with realistic mathematics education

To cite this article: H Julie 2018 J. Phys.: Conf. Ser. 1088 012044

View the article online for updates and enhancements.

### You may also like

- Lithium Tris[3-fluoro-1,2-benzenediolato(2-)-O, O]phosphate as a Novel Lithium Salt for Lithium Battery Electrolytes
   Noritoshi Nanbu, Koji Tsuchiya, Takatsugu Shibazaki et al.
- Averaged Lemaître—Tolman—Bondi dynamics
   Eddy G Chirinos Isidro, Rodrigo M Barbosa, Oliver F Piattella et al.
- Towards statistically homogeneous and isotropic perfect fluid universes with cosmic backreaction S M Koksbang



### Developing LTBI for addition and multiplication rules in probability theory with realistic mathematics education

### H Julie

Sanata Dharma University, Jl. Affandi Tromol Pos 29, Mrican, Daerah Istimewa Yogyakarta 55002 Indonesia

E-mail: hongkijulie@yahoo.co.id

Abstract. There were three components on a hypothetical learning trajectory (HLT) developed in this paper, namely: (1) the learning goal, (2) the learning activities, and (3) the way of students' thinking and learning. A learning trajectory based instruction (LTBI) was defined as a teaching and learning trajectory using HLT for instructional decisions. In this paper, the researcher will present a LTBI using Realistic Mathematics Education approach which helps mathematics education students following the Probabilistic Theory course to construct (1) the addition rule, and (2) the multiplication rule. The type of the research was the design research developed by Gravemeijer and Cobb. There were three phases in the research development, namely (1) the design preparation, (2) the design trial, and (3) the retrospective analysis. The researcher exposure in this paper was limited to the first stage of the design research developed by Gravemeijer and Cobb. As the products developed in this paper was limited to LTBI, so to construct a local instructional theory (LIT) for the sum and multiplication rules, the researcher needs to implement this LTBI in the classroom learning process.

### 1. Introduction

One of the mathematics courses that must be taken by students in Mathematics Education in the third semester is the probability course. The goal of this course is to help students to reinvent the basic probability concepts, and to apply these concepts to solve probabilistic problems. One of the importance of this subject was as it contained a provision for them to develop teaching and learning process about probability theory for senior high school students and/or vocational school students. From the lecture's experience of previous years, the most difficulties experienced by students were to perform a horizontal and vertical mathematizing process [1].

According to Sztajn et al. [2], Simon was the first researcher to use the term hypothetical learning trajectory (HLT) to represent the student learning process [2]. Simon (1995) said three components on a HLT, namely: (1) the learning goal, (2) the learning activities, and (3) how students think and learn. Simon named a trajectory as a hypothetical learning trajectory because the student's learning trajectory was unknowable [3].

The learning and the teaching were often looked at as two sides of the same phenomenon, but often the studies carried out in these two areas were not connected to one another [2]. One attempt to link the research in both fields appeared in 2012 conducted by Sztajn et al [2]. Their effort to combine study in both areas was to construct what they referred to as learning trajectory based instruction (LTBI). A LTBI was defined as a teaching and learning trajectory that HLT used for instructional decisions [2].

Content from this work may be used under the terms of the Creative Commons Attribution 3.0 licence. Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI.

The students' achievement taught by primary teachers were related directly and positively with mathematical and pedagogy abilities of their teachers [4,5]. There was a significantly connected between the knowledge achieved by the students and (1) the paradigm of teachers of mathematics teaching and learning process, and (2) teachers' care to the tendency of students' mathematics skills [4,5]. The mathematical knowledge of teachers related to the teachers' care of the tendency of students' mathematical skills [4,5]. The teacher mastery of the mathematics knowledge and the pedagogy would support the teachers' paradigm on the settlement of mathematical models and learning organization [4,5]. So, one of the determinants of student success in developing the probabilistic knowledge was the teacher' ability in managing the mathematics teaching and learning process and solving mathematical problems.

There were two types of understanding that students had in the process of learning mathematics, namely: (1) the instrumental understanding and (2) the relational understanding. The instrumental understanding means knowing how to use a rule or know how to use a formula to solve a problem, without understanding how the formula is derived, and why it can be used to solve the problem. Understanding in the relational understanding means knowing about (1) the relationship between concepts in mathematics (2) how to use a rule, (3) how to use a formula to solve a problem, (4) how the formula is derived, and (5) how to use a formula why the formula can be used to solve the problem [6].

From several studies reported that in the 21st century that humans not only required a content knowledge, but they also required skills that called as 21st-century skills. The 21st skills include the critical thinking and problem solving, creativity and innovation, communication and collaboration, flexibility and adaptability, initiative and self-direction, social and cross-cultural, productivity and accountability, leadership and responsibility, and information literacy [7,8]. In this LTBI, the developing of the critical thinking and problem solving were to become the focus of the researcher.

The philosophy of RME was mathematics as a human activity. It meant learning mathematics should be able to make the students thought that there was mathematics in human activities, and mathematics was used by them in real life [9,10,11]. There were five main characteristics in the RME [9,10,11], namely: (1) phenomenological exploration, (2) bridging by vertical instruments, (3) student contributions, (4) interactivity, and (5) intertwining.

According to Gravemeijer and Cobb [12], design research can be characterized as:

- Interventionist: the research leading to the design of an intervention in the real world.
- Iterative: the research incorporates a cyclic approach to the design, evaluation, and revision.
- Process-oriented: a model of research that avoids the measurement of inputs and outputs, focus on understanding and improving interventions.
- Oriented to usability: the benefits of design were measured by looking at the practicality of the design for the user in reality.
- Oriented to the theory: design (at least partially) made by theories that already exist, and field testing of the design contribute to the development of the theory.

According to Gravemeijer and Cobb [12], there were three phases in the design research, namely: (1) preparation of trial design, (2) trial design, and (3) a retrospective analysis [1]. In this paper, researchers will only discuss the results of research in stage 1.

The research question that would be answered by the researcher in this paper, namely: how to develop LTBI that could be used to build student knowledge about addition and multiplication rule using the RME approach?

### 2. Method

This research was classified as the design research. In this study, the researcher developed a LTBI to be used to build student knowledge concerning the addition and multiplication rule using RME approach. The research will only discuss the results at stage 1.

The subjects of this research were 38 students (7 male and 31 female) taking the Introduction Probability Theory course in one of the class at Sanata Dharma University. The research instrument used to obtain data about the students' reflection examined using the open questionnaire administered to students once the course completed. A teacher's journal was used to get data concerning teacher's reflection.

The study consisted of three cycles. Each cycle consisted of five main elements, namely context, experience, action, reflection, and evaluation. The learning process in the first cycle discussed about the counting principle, permutation and combination, experiment, sample space and events as well as the notion of the probability of the event and the definition of the axiomatic probability, the probability properties, independent and conditional events, and the conditional probability. The learning process in the second cycle discussed about random variables. The learning process in the third cycle concerned about the binomial, the Poisson, and the normal distribution. This paper is limited only at a LTBI that will help students to construct knowledge concerning addition and multiplication rules in the first cycle.

### 3. Result and discussion

In this paper, the researcher will develop a LTBI that will help students to construct knowledge about addition and multiplication rules. The learning goals of this LTBI were (1) students could reinvent the addition rule, and (2) students could reinvent the multiplication rule. The teaching and learning trajectory which content the learning activities and the way of students thinking and learning in the researcher's LTBI as followed:

• Students are required to solve the first problem in a way that they understand as follows: there are four green balls, and five red balls in a bag. From inside the bag, two balls will be taken at once. Please, determine how many possible outcomes from the ball-taking experiment!

Problem 1 is intended to provide an opportunity for students to explore a phenomenon that will encourage students to construct knowledge of the rules of addition and multiplication. This activity is planned by the researcher to bring up a phenomenological exploration characteristic.

### The first possibility of a student answer for the problem 1 is:

Suppose, the green balls in the bag are  $H_1$ ,  $H_2$ ,  $H_3$ ,  $H_4$ , and the red balls in the bag are  $M_1$ ,  $M_2$ ,  $M_3$ ,  $M_4$ ,  $M_5$ ; then

- O Students will make the following list to state the number of events for two green balls as follows:  $H_1H_2$ ,  $H_1H_3$ ,  $H_1H_4$ ,  $H_2H_3$ ,  $H_2H_4$ ,  $H_3H_4$ . So, the number of events for two green balls is six.
- O Students make the following list to state the number of events of one green ball and one red ball as follows:
  - $H_1M_1$ ,  $H_1M_2$ ,  $H_1M_3$ ,  $H_1M_4$ ,  $H_1M_5$ ,  $H_2M_1$ ,  $H_2M_2$ ,  $H_2M_3$ ,  $H_2M_4$ ,  $H_2M_5$ ,  $H_3M_1$ ,  $H_3M_2$ ,  $H_3M_3$ ,  $H_3M_4$ ,  $H_3M_5$ ,  $H_4M_1$ ,  $H_4M_2$ ,  $H_4M_3$ ,  $H_4M_4$ ,  $H_4M_5$ . So, the number of events for one green ball and one red ball is 20.
- O Students make the following list to state the number of events for two red balls:  $M_1M_2$ ,  $M_1M_3$ ,  $M_1M_4$ ,  $M_1M_5$ ,  $M_2M_3$ ,  $M_2M_4$ ,  $M_2M_5$ ,  $M_3M_4$ ,  $M_3M_5$ ,  $M_4M_5$ . So, the number of events for two red balls is 10.

Thus, the number of events in this experiment is 6 + 20 + 10 = 36.

### The second possibility of a student answer for the problem 1 is:

Suppose, the green balls in the bag are  $H_1$ ,  $H_2$ ,  $H_3$ ,  $H_4$ , and the red balls in the bag are  $M_1$ ,  $M_2$ ,  $M_3$ ,  $M_4$ ,  $M_5$ ; then

• The number of events for two green balls can be described with the diagram as follows (look at figure 1):

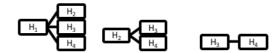


Figure 1. The possibility for two green balls.

So, the number of events for two green balls is 3 + 2 + 1 = 6

• The number of events for one green ball and one red ball can be drawn with the diagram as follows (look at figure 2):

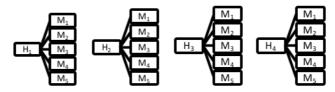


Figure 2. The possibility for one green ball and one red ball.

So, the number of events for one green ball and one red ball  $i_S(1\times5)+(1\times5)+(1\times5)+(1\times5)=4\times(1\times5)=4\times5=20$ .

o Figure 3 describes the number of events for two red balls.



**Figure 3.** The possibility for two red balls.

So, the number of events for two green balls is 4 + 3 + 2 + 1 = 10.

So, the number of possibilities in this experiment is 6 + 20 + 10 = 36.

### The third possibility of a student answer for the problem 1 is:

Suppose, the green balls in the bag are  $H_1$ ,  $H_2$ ,  $H_3$ ,  $H_4$ , and the red balls in the bag are  $M_1$ ,  $M_2$ ,  $M_3$ ,  $M_4$ ,  $M_5$ ; then

• Students will create the following chart to record the number of events for two green balls (look at table 1):

**Table 1.** The possibility for two green balls.

	$H_1$	$H_2$	$H_3$	$H_4$
$H_1$	-	$H_1H_2$	$H_1H_3$	$H_1H_4$
$\boldsymbol{H}_2$	-	-	$H_2H_3$	$H_2H_4$
$H_3^-$	-	-	-	$H_3H_4$
$H_4$	-	-	-	-

So, the number of events for two green balls is 1 + 2 + 3 = 6.

• Students will create the following table to record the number of events for one green ball and one red ball (look at table 2):

**Table 2.** The possibility for one green ball and one red ball.

	$M_1$	$M_2$	$M_3$	$M_4$	$M_5$
$H_1$	$H_1M_1$	$H_1M_2$ ,	$H_1M_3$	$H_1M_4$	$H_1M_5$
$\boldsymbol{H}_2$	$H_2M_1$	$H_2M_2$	$H_2M_3$	$H_2M_3$	$H_2M_5$
$H_3$	$H_2M_5$	$H_3M_2$	$H_3M_3$	$H_3M_4$	$H_3M_5$
$H_4$	$H_4M_1$	$H_4M_2$	$H_4M_3$	$H_4M_4$	$H_4M_5$

So, the number of events for one green ball and one red ball is  $4 \times 5 = 20$ .

Students will create the following table to record the number of events for two red balls (look at table 3):

**Table 3.** The possibility for two red balls.

	$M_1$	$M_2$	$M_3$	$M_4$	$M_5$
$M_1$	-	$M_1M_2$ ,	$M_1M_3$	$M_1M_4$	$M_1M_5$
$M_2$	-	-	$M_2M_3$	$M_2M_3$	$M_2M_5$
$M_3^-$	-	-	-	$M_3M_4$	$M_3M_5$
$M_4$	-	-	-	-	$M_4M_5$
$M_5$	_	_	_	_	-

So, the number of events for two red balls is 4 + 3 + 2 = 1 = 10.

So, the number of possibilities in this experiment is 6 + 20 + 10 = 36.

The researcher provides the opportunity for students to solve the problem individually so that researchers can bring up a student contribution characteristic in the LTBI design.

- Once the student completed this problem, they are asked to discuss their solution with a friend's seat. The researcher gave the opportunity for students to present their solution to their colleague so that the researcher brings up an interactivity characteristic in the LTBI design.
- The lecturer asks the student who answers like the first, second, and third possibility for the problem 1 to write his/her answer on the board. This step is designed so that the researcher can generate a bridging by vertical instrument characteristics in the LTBI design.
- Other students are asked to observe and criticize their friends' answers. The researcher can create a student contribution characteristic in the LTBI design with this activity.
- Students are required to solve the second problem in a way that they understand individually: in SMP Maju Jaya, there is an election of OSIS management. There are four candidates. From the four people selected three people to occupy the position of chairman, secretary, and treasurer. The rule of the election is a person should not obtain multiple positions. How many forms of organizational structure can be made?

The problem 2 is intended to provide an opportunity for students to explore a phenomenon that will encourage students to construct knowledge of the rules of multiplication. This activity is planned by researchers to create a phenomenological exploration characteristic.

### The first possibility of a student answer for the second problem is:

Suppose the 4 candidates are A, B, C, and D. Students write the following list as possible of OSIS stewardship arrangement: ABC, ABD, ACB, ACD, ADB, ADC, BAC, BAD, BCA, BCD, BDA, BDC, CAB, CAD, CBA, CBD, CDA, CDB, DAB, DAC, DBA, DBC, DCA, and DCB. Thus, there are 24 possible arrangements of OSIS management in Maju Jaya Junior High School.

### The second possibility of a student answer for the second problem is:

Suppose the four candidates are A, B, C, and D. Students describe the following diagram to illustrate the possibility of OSIS stewardship (look at figure 4):

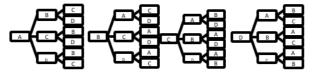


Figure 4. The possibility of OSIS stewardship.

Thus, the number of possible arrangements of OSIS management in SMP Maju Jaya is  $(3\times2) + (3\times2) + (3\times2) + (3\times2) = 4\times(3\times2) = 4\times3\times2 = 24$ .

### The third possibility of a student answer for the second problem is:

Suppose the four candidates are A, B, C, and D. Students describe the following table to illustrate the possibility of OSIS stewardship (refertoTable 4):

**Table 4.** The possibility of OSIS stewardship.

Chairman	Secretary	Treasurer
Four possibility	Three possibility	Two possibility

So, the possibilities of OSIS stewardship in Maju Jaya Junior High School are  $4\times3\times2=24$ . The researcher provides the opportunity for students to solve the problem individually so that researchers can bring up a student contribution characteristic in the LTBI design.

- Once the student completed this problem, they are asked to discuss their solution with a friend's seat. The researcher gave the opportunity for students to present their solution to their colleague so that the researcher brings up an interactivity characteristic in the LTBI design.
- The lecturer asks the student who answers like the first, second, and third possibility for the problem 2 to write his/her answer on the board. This step is designed so that the researcher can generate a bridging by vertical instrument characteristics in the LTBI design.
- Other students are asked to observe and criticize their friends' answers. The researcher can create a student contribution characteristic in the LTBI design with this activity.
- Students are invited to discuss about (1) the connecting between the concepts that have been built by them when studying set theory and number theory and problem 1 and 2 and (2) concluding about the addition and multiplication rules. The expected conclusions are as follows:
  - O The principle of addition: if the object  $A_1$  can be selected by  $n_1$  ways, the object  $A_2$  can be selected by  $n_2$  ways, until to object  $A_k$  can be selected by  $n_k$  ways, then the number of ways to choose objects  $A_1, A_2, \ldots$ , or  $A_k$  is  $n_1 + n_2 + \ldots + n_k$ .
  - O The Multiplication Principle: if a process can be formed from  $n_1$  different ways followed by the next process inside  $n_2$  different ways, and followed by the next process inside  $n_3$  different ways, up to the k-th procedure formed from  $n_k$  different ways, then the number of ways to form the procedure is  $n_1 \times n_2 \times ... \times n_k$ .
- The lecturer gives the exercise to be done by the students to strengthen the student' understanding about the rule of addition and multiplication. Here are two practical exercises that students can use to reinforce their understanding of the sum and multiplication rules:
  - Two judges for the mathematics Olympiad were chosen from four people. Three judges for the Olympiad physics contest were selected from six people. "How many ways can you choose to choose a jury of a mathematics Olympiad or a physics Olympiad jury?" and "How many ways can you choose to choose a jury of a mathematics Olympiad and a physics Olympiad jury?"
  - O The teacher will form a learning group consisting of four students from eight male students and four female students. How many study groups may be created by the teacher if in each group there are at least two male students?
- Lecturers hold class discussions to discuss student completion outcomes.

### 4. Conclusion

Three conclusions can be drawn from the above explanation, namely:

• To develop a LTBI to help students constructing the addition and multiplication rules using the RME approach, the researcher needs to conduct the several steps. First, providing the phenomenon to be explored by the student. Second, providing the opportunity for students to discuss with their friends. Third, asking the students to present the answers according to the

- formalization degree of the answers. Fourth, inviting students in class discussions to connect new material with the concepts they have learned and drawn conclusions.
- The contexts of ball-taking experiments and OSIS selection are used by researchers to help students construct their knowledge about the addition and multiplication rules.
- The RME approach can be used to assist students in constructing knowledge about the rules of addition and multiplication.

### References

- [1] Julie H 2017 AIP Conference Proceedings vol 1868 (US: AIP Publishing)
- [2] Sztajn P, Confrey J, Wilson P H and Edgington C 2012 Learning trajectory based instruction: toward a theory of teaching *Educational Researcher* **41** 147
- [3] Simon M A 1995 Reconstructing mathematics pedagogy from a constructivist perspective Journal for Research in Mathematics Education 26 114
- [4] Campbell P F, Nishio M, Smith T M, Clark L M, Conant D L, Rust A H, ... and Choi Y 2014
  The Relationship Between Teachers' Mathematical Content and Pedagogical Knowledge,
  Teachers' Perceptions, and Student Achievement *Journal for Research in Mathematics*Education 45 419
- [5] Julie H 2017 The elementary school teachers' ability in adding and subtracting fraction, and interpreting and computing *International Journal of Science and Applied Science:*Conference Series 1 55
- [6] Skemp R 2009 *The Psychology of Learning Mathematics* (New York: Routledge)
- [7] Ariyadi W 2016 Students' Information Literacy: A Perspective from Mathematical Literacy *IndoMS Journal Mathematics Education* 7 73
- [8] Stacey K 2011 The PISA View of Mathematical Literacy in Indonesia *Journal Mathematics Education* **2** 95
- [9] Gravemeijer K P G 1994 Developing Realistic Mathematics Education (Utrecht: Freudenthal Institute)
- [10] Julie H 2015 Student learning materials on the multiplication and division of fractions for grade five with realistic mathematics education *Proceedings of the 3th SEA–DR conference* (Palembang: Universitas Sriwijaya)
- [11] Julie H 2016 Developing student learning materials on the multiplication fractions for grade five with realistic mathematics education *Proceedings of the 4th SEA–DR conference* (Padang: Universitas Negeri Padang)
- [12] Van Den Akker J, Gravemeijer K, McKenney S and Nieveen N 2006 Educational Design Research (New York: Routledge)



# AWARDED TO

HONGKI JULIE

# PRESENTER

IN THE 6th SOUTH EAST ASIA DESIGN RESEARCH INTERNATIONAL CONFERENCE 27<sup>th</sup> - 28<sup>th</sup> June 2018, Syiah Kuala University

Banda Aceh, Indonesia

Rector of Syiah Kuala University

rof. Dr. Ir. Samsul Rizal, MEng. NIP. 196208081988031003

Head of Organizing Committee

MP. 197011171998032002 Dr. Rahmah Johar, M.Pd.



SOUTH EAST ASIA DESIGN RESEARCH

INTERNATIONAL CONFERENCE













